

Heavy flavour production at ATLAS

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Joint Institute for Nuclear Research



Heavy-quark hadroproduction from collider to astroparticle physics
Mainz Institute for Theoretical Physics, Johannes Gutenberg University, Germany
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B-physics at ATLAS

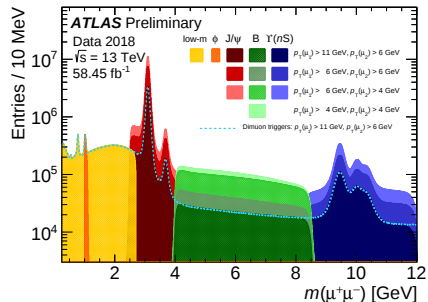
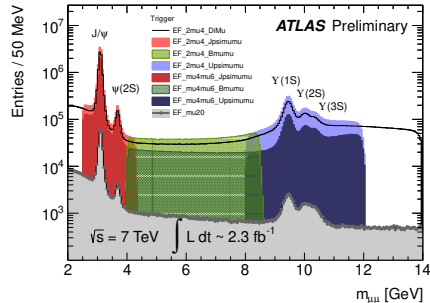
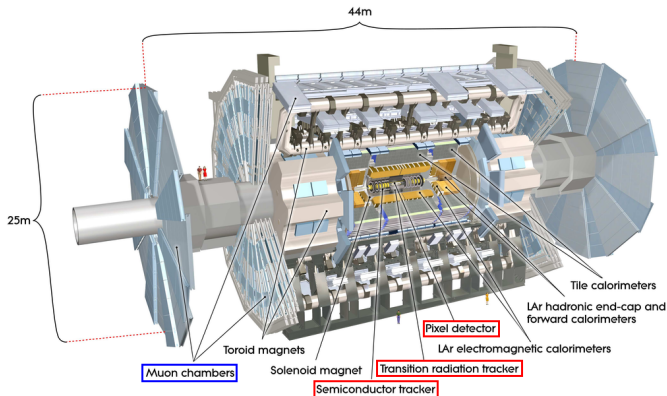
- ▶ Possible to measure heavy flavour (HF) production at *highest possible energies*
- ▶ Much *higher HF yields* in *pp* environment compared to B-factories
- ▶ Possible to produce *all possible heavy states* → extended spectroscopy studies
- ▶ ATLAS and CMS, although not specially optimized for B-physics, provide *complementary kinematic region to LHCb*
 - ▶ Benefit from *higher statistics* in certain analyses
- ▶ This talk covers a selection of ATLAS results on heavy flavour production of few years
 - ▶ Impossible to cover all interesting studies at once + a bit untypical scope of the Workshop
 - ▶ → **Feel free to ask and discuss offline!**

- ▶ ATLAS detector
- ▶ Open heavy flavour production
 - ▶ Charmed meson production at 7 TeV – Nucl. Phys. B 907 (2016) 717 [↗](#)
 - ▶ b hadron pair production measurement at 8 TeV – JHEP 11 (2017) 62 [↗](#)
 - ▶ ★ Relative B_c^+/B^+ production measurement at 8 TeV – paper in preparation
- ▶ Hidden heavy flavour production
 - ▶ ★ High- p_T J/ψ and $\psi(2S)$ production at 13 TeV paper in preparation
 - ▶ Heavy quarkonium production in pPb (Eur. Phys. J. C 78 (2018) 171 [↗](#)) and $PbPb$ (Eur. Phys. J. C 78 (2018) 762 [↗](#))
 - ▶ ★ Search for pentaquarks in $J/\psi p$ system from $\Lambda_b \rightarrow J/\psi p K^+$ decays – preliminary conference note in preparation

★ – brand-new results released just this week for Beauty conference!

ATLAS detector and trigger for B-physics

- Inner Detector in solenoid field for reconstructing tracks and vertices
- Muon Spectrometer in toroid field for muon identification
- Trigger selection primarily based on di-muon signature



Motivation

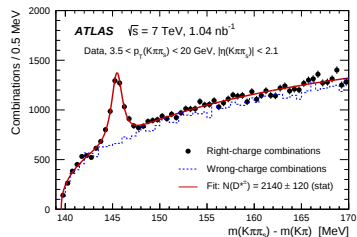
- ▶ Heavy quark production measurement at LHC $\rightarrow$ test of pQCD calculations at highest possible energies
 - ▶ Charmed mesons are produced in *charm hadronization* and *b hadron decays*
- ▶ Various theoretical approaches available
 - ▶ Fixed-order + next-to-leading-logarithm (FONLL) predictions
 - ▶ General-mass variable-flavour-number-scheme (GM-VFNS) calculations
 - ▶ NLO QCD calculations matched to LL parton-shower MC
 - ▶ MC@NLO matched to HERWIG
 - ▶ POWHEG matched to HERWIG or PYTHIA

Scope of the study

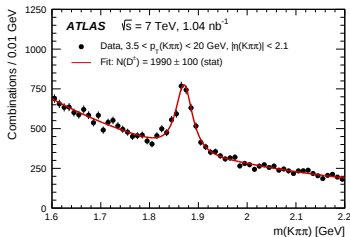
- ▶ Three D mesons measured: D^{*+} , D^+ , D_s^+
- ▶ Kinematic region of the x-section measurement:
 - ▶ $3.5 < p_T(D) < 100$ GeV
 - ▶ $|\eta(D)| < 2.1$
- ▶ Data of 2010 at $\sqrt{s} = 7$ TeV are used
 - ▶ 1.04 nb^{-1} collected with minimum-bias triggers used for $p_T < 20$ GeV range
 - ▶ 280 nb^{-1} with jet triggers for $20 < p_T < 100$ GeV range

D meson reconstruction

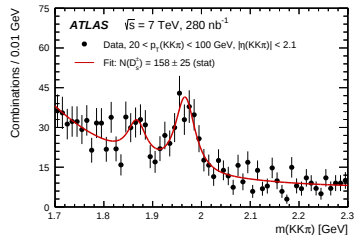
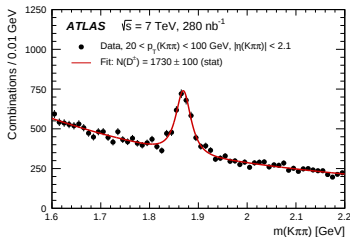
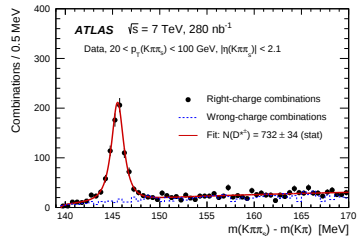
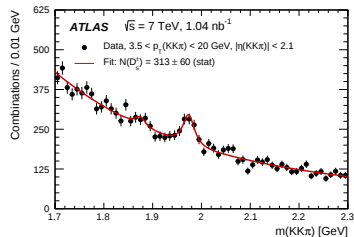
$$D^{*+} \rightarrow D^0 \pi_s^+ \rightarrow (K^- \pi^+) \pi_s^+$$



$$D^+ \rightarrow K^- \pi^+ \pi^+$$



$$D_s^+ \rightarrow \phi \pi^+ \rightarrow (K^+ K^-) \pi^+$$



π_s^+ – soft pion

Results: visible cross-sections

► Visible cross-sections measured:

	$\sigma^{\text{vis}}(D^{*\pm})$		$\sigma^{\text{vis}}(D^{\pm})$		$\sigma^{\text{vis}}(D_s^{*\pm})$	
Range	low- p_T	high- p_T	low- p_T	high- p_T	low- p_T	high- p_T
[units]	[μb]	[nb]	[μb]	[nb]	[μb]	[nb]
ATLAS	331 ± 36	988 ± 100	328 ± 34	888 ± 97	160 ± 37	512 ± 104
GM-VFNS	340^{+130}_{-150}	1000^{+120}_{-150}	350^{+150}_{-160}	980^{+120}_{-150}	147^{+54}_{-66}	470^{+56}_{-69}
FONLL	202^{+125}_{-79}	753^{+123}_{-104}	174^{+105}_{-66}	617^{+103}_{-86}	-	-
POWHEG+PYTHIA	158^{+179}_{-85}	600^{+300}_{-180}	134^{+148}_{-70}	480^{+240}_{-130}	62^{+64}_{-31}	225^{+114}_{-69}
POWHEG+HERWIG	137^{+147}_{-72}	690^{+380}_{-160}	121^{+129}_{-64}	580^{+280}_{-140}	51^{+50}_{-25}	268^{+107}_{-62}
MC@NLO	157^{+125}_{-72}	980^{+460}_{-290}	140^{+112}_{-65}	810^{+390}_{-260}	58^{+42}_{-25}	345^{+175}_{-87}

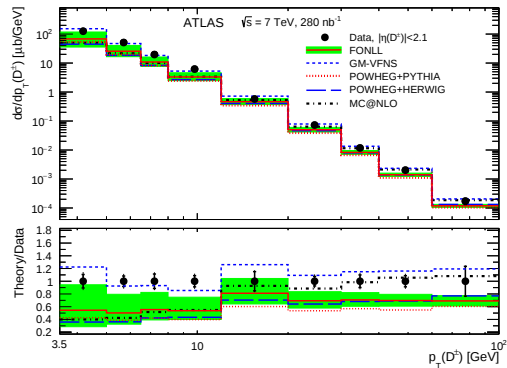
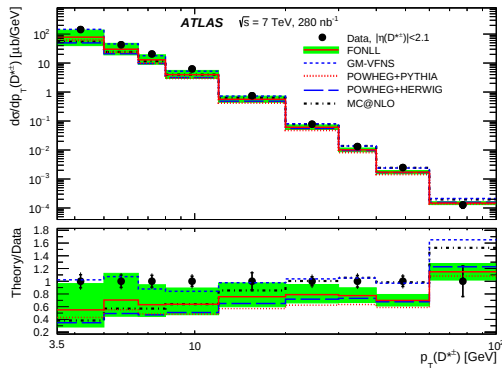
► Statistical and systematics uncertainties generally of the same order

► Tracking efficiency, luminosity and branching fractions are the main systematics sources

► GM-VFNS approach shows the best description of data

► FONLL and NLO+PS approaches are generally below data, but still consistent within uncertainties

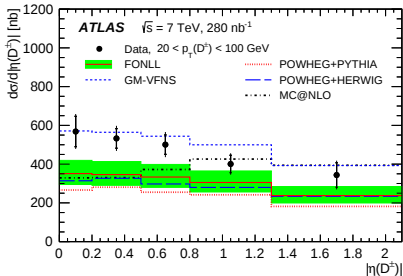
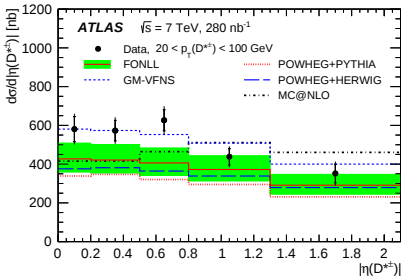
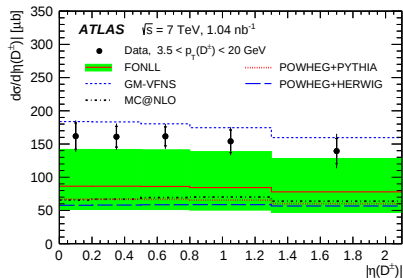
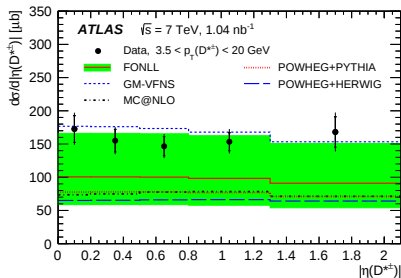
Results: differential cross-sections – p_T



- ▶ GM-VFNS describes well both shape and normalization
- ▶ FONLL and NLO+PS are still consistent with data
- ▶ MC@NLO predicts harder p_T spectrum than in data

Results: differential cross-sections – η

- **GM-VFNS** shows again a better description
- **MC@NLO** predicts a different η shape in the high- p_T range



Results: extrapolation

- ▶ For extrapolation to the full phase space, *FONLL* predictions are used (including subtraction of $b \rightarrow c$ contribution)
 - ▶ POWHEG+PYTHIA are used for extraction of fragmentation ratios
- ▶ Full $c\bar{c}$ production x-section:

$$\sigma_{c\bar{c}}^{\text{tot}} = 8.6 \pm 0.3 (\text{stat}) \pm 0.7 (\text{syst}) \pm 0.3 (\text{lum}) \pm 0.2 (\text{ff})_{-3.4}^{+3.8} (\text{extr}) \text{ mb}$$

- ▶ Good agreement with ALICE measurement
- ▶ Charm fragmentation ratios:

$$\gamma_{s/d} = 0.26 \pm 0.05 (\text{stat}) \pm 0.02 (\text{syst}) \pm 0.02 (\text{br}) \pm 0.01 (\text{extr}),$$

$$P_v^d = 0.56 \pm 0.03 (\text{stat}) \pm 0.01 (\text{syst}) \pm 0.01 (\text{br}) \pm 0.02 (\text{extr}).$$

- ▶ Good agreement with ALICE, HERA (ep) measurements and LEP averages
 - ▶ P_v^d is smaller than expectation from naive spin-counting (0.75)
 - ▶ Questions the HQET assumption on charm fragmentation
 - ▶ Also slightly smaller than string fragmentation and thermodynamical approach predictions
- (2/3)

Overall uniquely advanced measurement for LHC general-purpose detectors!

- ▶ A number of recent measurement of b production highlighted certain disagreements between models and data
- ▶ Especially $b\bar{b}$ production at small open angles is *sensitive to the details of various calculations*, but only *loosely constrained experimentally*
- ▶ Studies of $H \rightarrow b\bar{b}$ much rely on modelling of $b\bar{b}$ production in this region
- ▶ Measure $b\bar{b}$ pair production
 - ▶ one b is identified via $H_b \rightarrow J/\psi + X$ decay (including feed-downs of heavier charmonia)
 - ▶ the other via $H_b \rightarrow \mu + Y$ (including cascades)
- ▶ Differential cross-sections are measured in
 - ▶ $\Delta\phi(J/\psi, \mu)$,
 - ▶ $p_T(J/\psi, \mu)$,
 - ▶ $\Delta R(J/\psi, \mu)$ overall and in bins of $p_T(J/\psi, \mu) < 20$ GeV and $p_T(J/\psi, \mu) > 20$ GeV,
 - ▶ $\Delta y(J/\psi, \mu)$,
 - ▶ average rapidity of J/ψ and μ , y_{boost} ,
 - ▶ $m(J/\psi, \mu)$
 - ▶ $p_T(J/\psi, \mu)/m(J/\psi, \mu)$ and its inverse
- ▶ 11.5 fb⁻¹ of $\sqrt{s} = 8$ TeV are used

- ▶ Fiducial volume definition:

- ▶ $p_T(\mu) > 6 \text{ GeV}$ for all three muons
- ▶ $|\eta(\mu)| < 2.3$ for the J/ψ muons and < 2.5 for the 3rd muon

- ▶ Full fiducial cross-section:

$$\sigma(B(\rightarrow J/\psi[\rightarrow \mu^+\mu^-] + X)B(\rightarrow \mu + X)) = 17.7 \pm 0.1(\text{stat}) \pm 2.0(\text{syst}) \text{ nb.}$$

- ▶ Comparison with various models are performed:

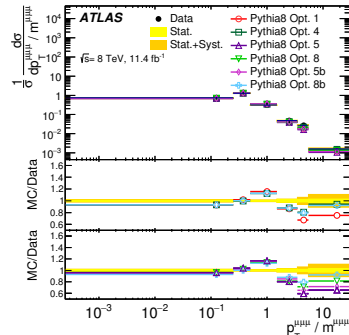
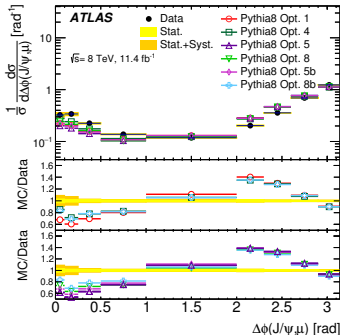
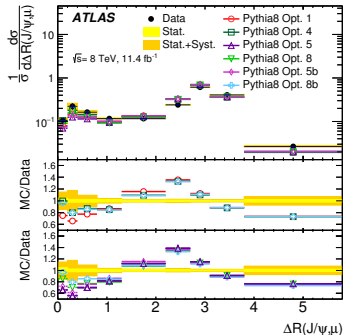
- ▶ PYTHIA 8
- ▶ HERWIG++
- ▶ MADGRAPH_AMC@NLOv2.2.2 interfaced to PYTHIA 8 (CKKW-L merging scheme with 15 GeV merging scale)
 - ▶ 4-FNS and 5-FNS modelling in MADGRAPH
- ▶ SHERPA 2.1.1 (5-FNS), merging with ME+PS@LO prescription

Test PYTHIA 8 gluon splitting kernels

- ▶ Test gluon splitting description
 - ▶ Is the scale of α_s in splitting set by relative p_T or by mass?
- ▶ 6 options for the splitting kernels in PYTHIA 8
- ▶ PYTHIA does not describe these shapes
 - ▶ p_T -based scale splitting kernels behave better for close-by $b\bar{b}$

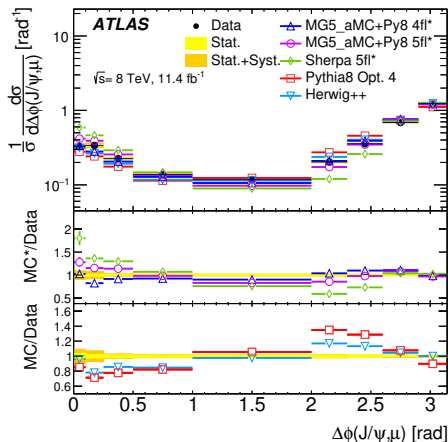
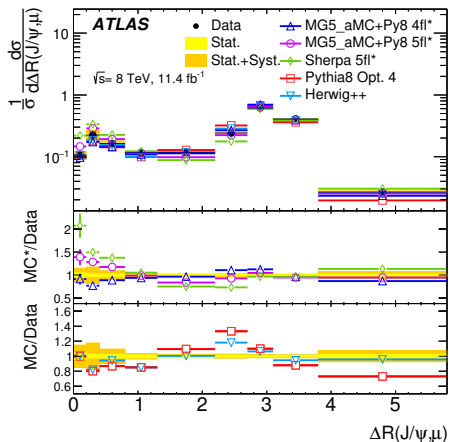
Option label	Descriptions
Opt. 1	The same splitting kernel, $(1/2)(z^2 + (1-z)^2)$, for massive as massless quarks, only with an extra β phase-space factor. This was the default setting in PYTHIA8.1, and currently must also be used with the MC@NLO [50] method.
Opt. 4	A splitting kernel $z^2 + (1-z)^2 + 8r_q z(1-z)$, normalised so that the z -integrated rate is $(\beta/3)(1+r/2)$, and with an additional suppression factor $(1 - m_{q\bar{q}}^2/m_{\text{dipole}}^2)^3$, which reduces the rate of high-mass $q\bar{q}$ pairs. This is the default setting in PYTHIA8.2.
Opt. 5	Same as Option 1, but reweighted to an $\alpha_s(km_{q\bar{q}}^2)$ rather than the normal $\alpha_s(p_T^2)$, with $k = 1$.
Opt. 5b	Same as Option 5, but setting $k = 0.25$.
Opt. 8	Same as Option 4, but reweighted to an $\alpha_s(km_{q\bar{q}}^2)$ rather than the normal $\alpha_s(p_T^2)$, with $k = 1$.
Opt. 8b	Same as Option 8, but setting $k = 0.25$.

Table 1: Description of PYTHIA8 options. Options 2, 3, 6 and 7 are less well physically motivated and not considered here. The notation used is as follows: $r_q = m_q^2/m_{q\bar{q}}^2$, $\beta = \sqrt{1 - 4r_q}$, with m_q the quark mass and $m_{q\bar{q}}$ the $q\bar{q}$ pair invariant mass.



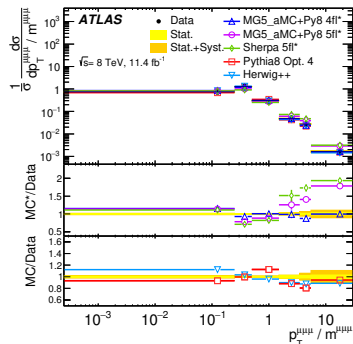
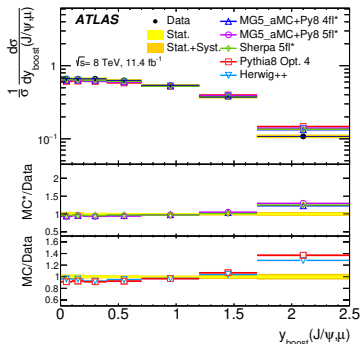
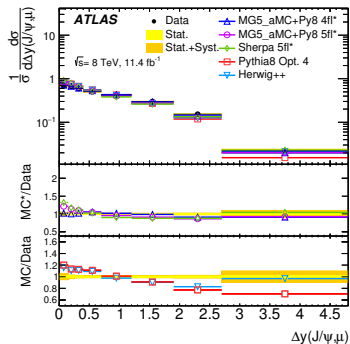
Test various model predictions (1)

- HERWIG++ reproduces ΔR and $\Delta\phi$ best
- 4-FNS works better for ΔR and $\Delta\phi$ than 5-FNS (deviate to opposite sides from data)
- SHERPA is similar to 5-FNS MG, but the description is worse overall



Test various model predictions (2)

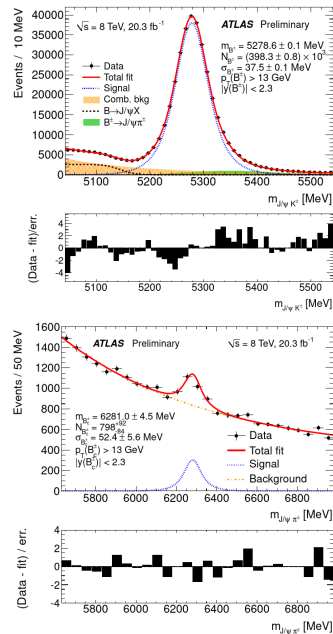
- ▶ MG and SHERPA demonstrate better agreement in Δy , PYTHIA and HERWIG++ worse
- ▶ In y_{boost} , a comparable picture across the predictions (expected to be sensitive to PDF)
- ▶ 4-FNS describes the high p_T/m region much better than 5-FNS; PYTHIA and HERWIG++ generally comparable



- ▶ **Very comprehensive measurement** of differential cross-section of $b\bar{b}$ production performed
 - ▶ in 10 kinematic observables
- ▶ Particularly sensitive to close-by $b\bar{b}$ pairs down to zero open angle
- ▶ Various predictions compared to data
 - ▶ different ME, PS models, 4-/5-flavour treatment; g splitting kernels
 - ▶ 4-FNS MADGRAPH_AMC@NLOv2.2.2 provides the best data description overall
 - ▶ PYTHIA and HERWIG++ are comparable and further tuning may improve data description
 - ▶ **theoretical uncertainties not evaluated in this study**
- ▶ *New test of QCD, motivate the choice of calculations used to model b hadron production and their further tuning*

Relative B_c^+ / B^+ production measurement at 8 TeV (paper in preparation)

- ▶ B_c^+ is the only known weakly decaying particle made of two heavy quarks
 - ▶ Unique probe for heavy quark dynamics
- ▶ Production involves simultaneous producing $b\bar{b}$ and $c\bar{c}$
 - ▶ Expected to be dominated by $gg \rightarrow B_c^+ + b + \bar{c}$
 - ▶ x-section predicted at level 0.2 % of inclusive $b\bar{b}$ production
- ▶ Measure the ratio: $\frac{\sigma(B_c^+) \cdot \mathcal{B}(B_c^+ \rightarrow J/\psi \pi^+)}{\sigma(B^+) \cdot \mathcal{B}(B^+ \rightarrow J/\psi K^+)}$
 - ▶ common systematic uncertainties mostly cancel
- ▶ Fiducial region of the measurement:
 - ▶ $p_T(B) > 13 \text{ GeV}$, $|y(B)| < 2.3$
- ▶ Measure total production and differential in $p_T(B)$ and $|y(B)|$



B_c^+ / B^+ production: results

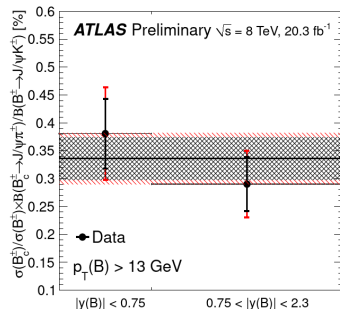
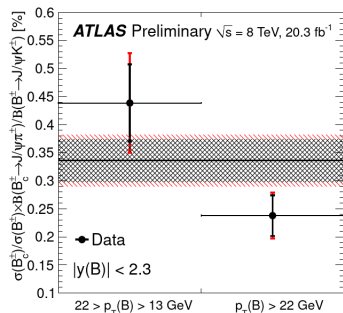
- Production ratio in the fiducial region

$$\frac{\sigma(B_c^+) \cdot \mathcal{B}(B_c^+ \rightarrow J/\psi \pi^+)}{\sigma(B^+) \cdot \mathcal{B}(B^+ \rightarrow J/\psi K^+)} =$$

$$(0.34 \pm 0.04(\text{stat.}) \pm 0.02(\text{syst.}) \pm 0.01 \text{ lifetime})$$

- Lower than the LHCb result [1] for more forward and lower- p_T fiducial volume
- Fairly consistent with the CMS result [2] in a similar (but not identical) volume
- B_c^+ production decreases faster with p_T than that for B^+
- No evident rapidity dependence

Analysis bin	$\sigma(B_c^\pm)/\sigma(B^\pm) \times \mathcal{B}(B_c^\pm \rightarrow J/\psi \pi^\pm)/\mathcal{B}(B^\pm \rightarrow J/\psi K^\pm)$
$p_T(B) > 13 \text{ GeV}, y(B) < 2.3$	$(0.34 \pm 0.04_{\text{stat}} \pm 0.02_{\text{syst}} \pm 0.01_{\text{lifetime}})\%$
$22 > p_T(B) > 13 \text{ GeV}, y(B) < 2.3$	$(0.44 \pm 0.07_{\text{stat}} \pm 0.04_{\text{syst}} \pm 0.01_{\text{lifetime}})\%$
$p_T(B) > 22 \text{ GeV}, y(B) < 2.3$	$(0.24 \pm 0.04_{\text{stat}} \pm 0.01_{\text{syst}} \pm 0.01_{\text{lifetime}})\%$
$p_T(B) > 13 \text{ GeV}, y(B) < 0.75$	$(0.38 \pm 0.06_{\text{stat}} \pm 0.04_{\text{syst}} \pm 0.01_{\text{lifetime}})\%$
$p_T(B) > 13 \text{ GeV}, 2.3 > y(B) > 0.75$	$(0.29 \pm 0.05_{\text{stat}} \pm 0.02_{\text{syst}} \pm 0.01_{\text{lifetime}})\%$

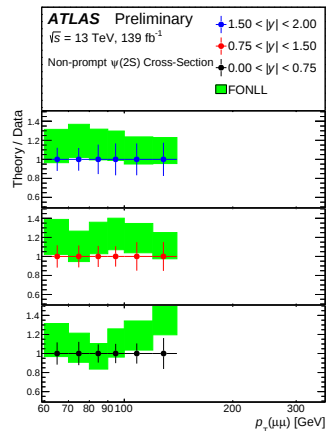
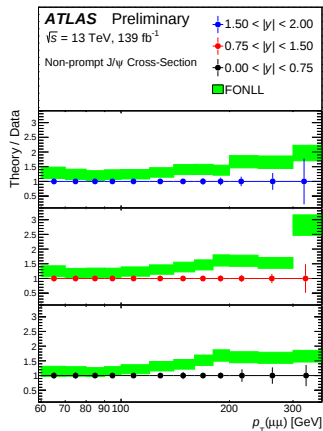
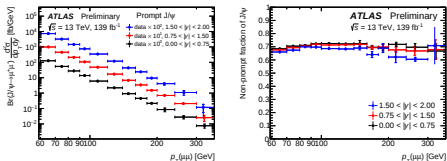


High- p_T J/ψ and $\psi(2S)$ production measurement (paper in preparation)

- ▶ Two different mechanisms for charmonium production:
 - ▶ *Prompt*: directly in pp interaction or via feed-down from heavier states
 - ▶ $\sim 35\%$ of J/ψ comes from feed-down; $\psi(2S)$ is produced almost directly
 - ▶ **Theory**: Non-Relativistic QCD (NRQCD) introduces a number of phenomenological parameters (LDMEs) extracted from Tevatron data fits
 - ▶ fails to build a comprehensive description
 - ▶ *Non-prompt*: from decays of b hadrons
 - ▶ Can be distinguished by fitting the pseudo proper lifetime
 - ▶ **Theory**: Fixed Order Next-to-Leading Logarithm (FONLL) perturbative $b\bar{b}$ production, data-driven fragmentation and b hadron decay model
- ▶ ATLAS measured before J/ψ and $\psi(2S)$ differential x-sections at 7, 8 TeV– **Eur. Phys. J. C 76 (2016) 283** 
- ▶ Overall reasonable agreement for both approaches
- ▶ New measurement focuses on high- p_T charmonia – **paper in preparation**
 - ▶ Use *single-muon* triggers (50 GeV muon p_T threshold) to cover the range 60–360 GeV
 - ▶ Full Run-2 dataset, **139 fb⁻¹** at 13 TeV
 - ▶ Double-differential x-section measurement

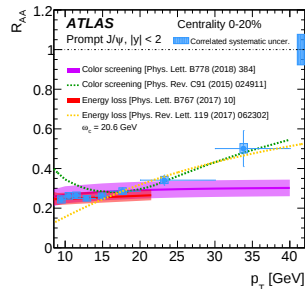
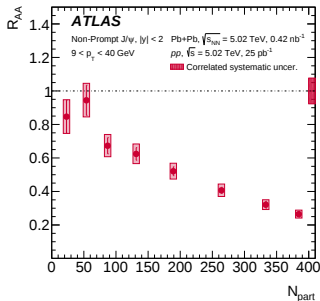
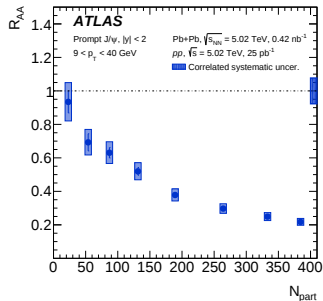
High- p_T J/ψ and $\psi(2S)$ measurement: results

- Measured are
 - Prompt and non-prompt J/ψ and $\psi(2S)$ x-sections
 - Non-prompt fraction for J/ψ and $\psi(2S)$
 - $\psi(2S)/J/\psi$ production ratio for prompt and non-prompt
- p_T ranges goes well beyond what was achieved so far
- FONLL consistent at low- p_T , over-estimates high- p_T production

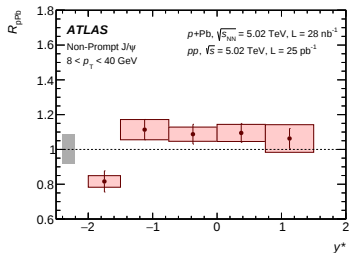
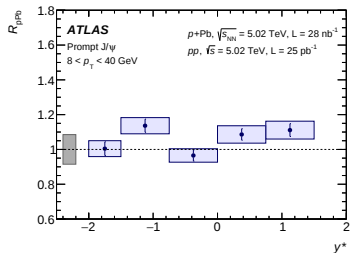
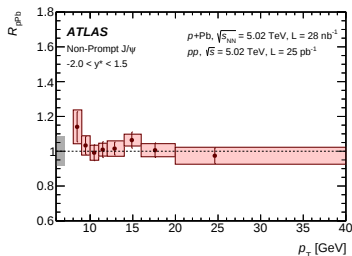
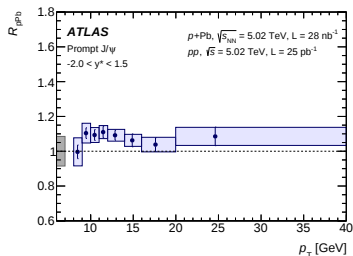


- Probe **deconfined quark-gluon plasma** in $A + A$ collisions
 - Suppression of *prompt* charmonia could provide info about temperature of deconfinement
 - Possible enhancement: new quarkonium formation mechanism ($c\bar{c}$ recombination in medium)
 - *Non-prompt* charmonia allows studying b quark propagation through the medium
 - Possibly different mechanism (collisions, radiation) from $c\bar{c}$ suppression (colour screening)

- J/ψ production strongly suppressed in central collisions
 - very similar for prompt and non-prompt
 - not quite expected, as the two cases have different origins
- R_{AA} increases at high $p_T > 12$ GeV for prompt J/ψ , flat for non-prompt



- $p + A$ collisions serve to disentangle **cold nuclear matter** effects (CNM)

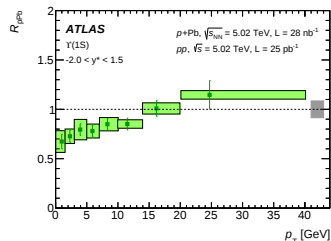


- R_{pPb} factors for prompt and non-prompt J/ψ consistent with unity

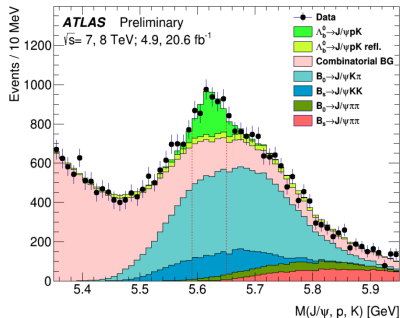
- no p_T or y^* dependence
- weak modification for J/ψ production due to CNM effects

- $R_{pPb} < 1$ for $\Upsilon(1S)$ below 15 GeV

- stronger nPDF shadowing for small x ?

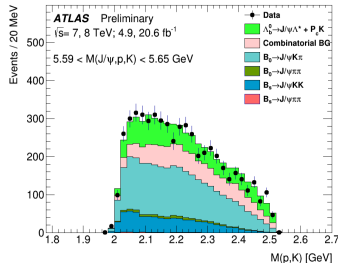
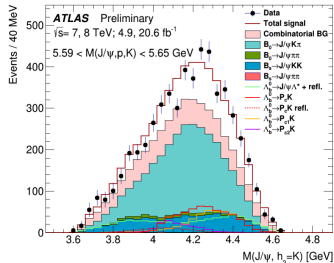
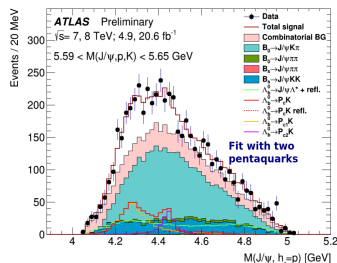
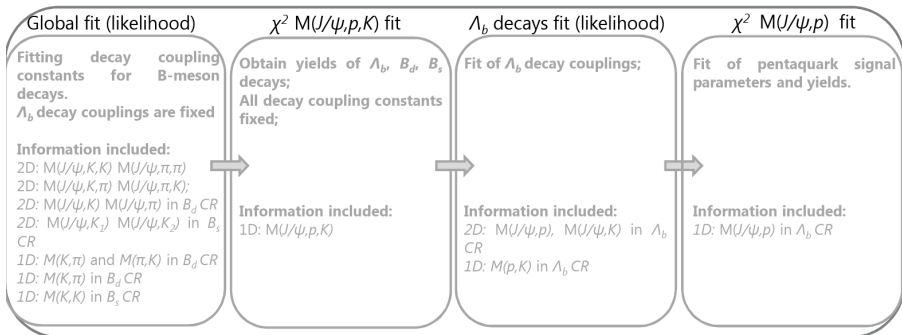


- ▶ Motivated by LHCb discovery of new resonances in $J/\psi p$ system from $\Lambda_b \rightarrow J/\psi p K^-$ decay
- ▶ **No particle-ID** in ATLAS – select $J/\psi h_1 h_2$ candidates where $h_{1,2}$ can be $p, K^\pm, \pi^\pm$
 - ▶ $\Lambda_b \rightarrow J/\psi p K^-$ via intermediate Λ^{*0} 's and P_c 's
 - ▶ $B^0 \rightarrow J/\psi K^+ \pi^-$ via intermediate K^{*0} 's and Z_c 's
 - ▶ $B^0 \rightarrow J/\psi \pi^+ \pi^-$ (via intermediate f^0 's and ρ 's)
 - ▶ $B_s^0 \rightarrow J/\psi K^+ K^-$ via intermediate f^0 and ϕ 's
 - ▶ $B_s^0 \rightarrow J/\psi \pi^+ \pi^-$ (via intermediate f^0 's and ρ 's)
- ▶ Simulation uses phase-space decays weighted with theoretical MEs
- ▶ To suppress light Λ^{*0} 's, K^{*0} 's, f^0 , ϕ 's, **remove events** with $M(\pi K)$ or $M(K\pi) < 1.55$ GeV



Search for pentaquarks: fit

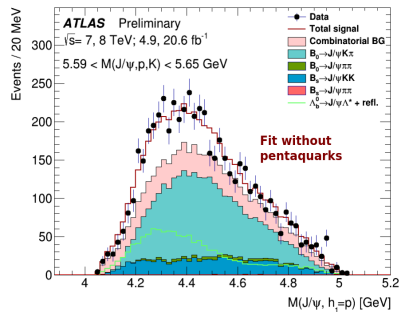
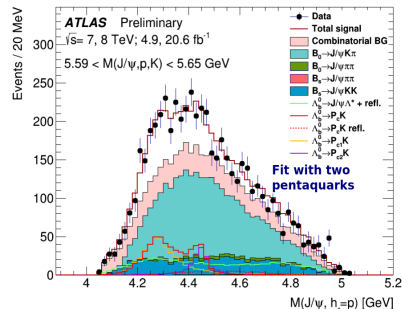
Fit uses signal region ($5.59 < m(J/\psi p K^-) < 5.65$ GeV) and two control regions for B^0 and B_s^0



Search for pentaquarks: results

- Data prefer the model with two pentaquarks:
 $\chi^2/\text{n.d.f.} = 37.1/39$, $p = 55.7\%$
 - Equally fine with four-pentaquarks hypothesis
 - Model w/o pentaquarks still not excluded:
 $\chi^2/\text{n.d.f.} = 42.0/23$, $p = 9.1 \cdot 10^{-3}$
- P_{c1} mass slightly lower than LHCb result
 - Fit with all masses and widths fixed to LHCb gives
 $\chi^2/\text{n.d.f.} = 49.0/43$, $p = 24.5\%$

Parameter	Value	LHCb value [5]
$N(P_{c1})$	$400^{+130}_{-140}(\text{stat})^{+110}_{-100}(\text{syst})$	—
$N(P_{c2})$	$150^{+170}_{-100}(\text{stat})^{+50}_{-90}(\text{syst})$	—
$N(P_{c1} + P_{c2})$	$540^{+80}_{-70}(\text{stat})^{+70}_{-80}(\text{syst})$	—
$\Delta\phi$	$2.8^{+1.0}_{-1.6}(\text{stat})^{+0.2}_{-0.1}(\text{syst})$ rad	—
$m(P_{c1})$	$4282^{+33}_{-26}(\text{stat})^{+28}_{-7}(\text{syst})$ MeV	$4380 \pm 8 \pm 29$ MeV
$\Gamma(P_{c1})$	$140^{+77}_{-50}(\text{stat})^{+41}_{-33}(\text{syst})$ MeV	$205 \pm 18 \pm 86$ MeV
$m(P_{c2})$	$4449^{+20}_{-29}(\text{stat})^{+18}_{-10}(\text{syst})$ MeV	$4449.8 \pm 1.7 \pm 2.5$ MeV
$\Gamma(P_{c2})$	$51^{+59}_{-48}(\text{stat})^{+14}_{-46}(\text{syst})$ MeV	$39 \pm 5 \pm 19$ MeV



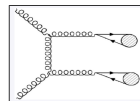
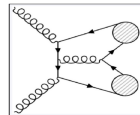
- ▶ A selection of ATLAS results on heavy flavour production was presented
 - ▶ Production of open charm and beauty
 - ▶ Physics of B_c^+ mesons
 - ▶ Conventional and exotic hidden charm states
 - ▶ *A few more interesting results on backup slides :-)*
 - ▶ **Do not hesitate to ask and discuss offline!**
- ▶ Many B-physics measurements are only based on Run-1 yet – the potential is nearly exhausted
- ▶ Full Run-2 dataset is still be be fully exploited – **stay tuned for many new results!**

- [1] LHCb Collaboration, *Measurement of B_c^+ Production in Proton-Proton Collisions at $\sqrt{s} = 8$ TeV*, *Phys. Rev. Lett.* 114 (2015) 132001 [↗](#)
- [2] CMS Collaboration, *Measurement of the ratio of the production cross sections times branching fractions of $B_c^\pm \rightarrow J/\psi \pi^\pm$ and $B^\pm \rightarrow J/\psi K^\pm$ and $B(B_c^\pm \rightarrow J/\psi \pi^\pm \pi^\pm \pi^\mp)/B(B_c^\pm \rightarrow J/\psi \pi^\pm)$ at $\sqrt{s} = 7$ TeV*, *JHEP* 01 (2015) 063 [↗](#)
- [3] ATLAS Collaboration, *Observation of an Excited $B_c^\pm$ Meson State with the ATLAS Detector*, *Phys. Rev. Lett.* 113 (2014) 212004 [↗](#)
- [4] LHCb Collaboration, *Search for excited B_c^+ states*, *JHEP* 01 (2018) 138 [↗](#)
- [5] CMS Collaboration, *Observation of Two Excited B_c^+ States and Measurement of the $B_c^+(2S)$ Mass in pp Collisions at $\sqrt{s} = 13$ TeV*, *Phys. Rev. Lett.* 122 (2019) 132001 [↗](#)
- [6] LHCb Collaboration, *Observation of an excited B_c^+ state*, *Phys. Rev. Lett.* 122 (2019) 232001 [↗](#)

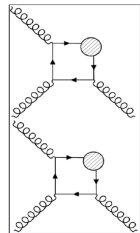
Backup slides

Prompt charmonium pair production

- ▶ Two principal possibilities to produce two objects in a pp collision:
- ▶ Single Parton Scattering (SPS)
- ▶ Double Parton Scattering (DPS)
 - ▶ effective cross-section σ_{eff} accounting for probability of the two processes to happen in a single pp collision: $\sigma_{\text{DPS}} = \frac{1}{2} \frac{\sigma(J/\psi)^2}{\sigma_{\text{eff}}}$
 - ▶ σ_{eff} is assumed to be universal across processes and energy scales
 - ▶ 12–20 mb values obtained earlier; however, indication of lower values from pair charmonia/bottommonia production questions the universality of σ_{eff}



SPS

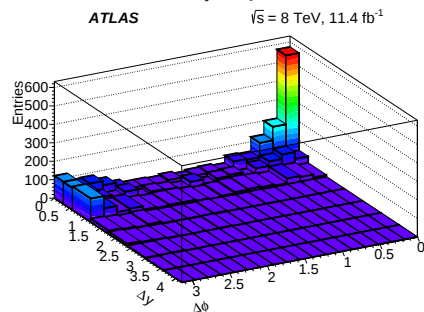
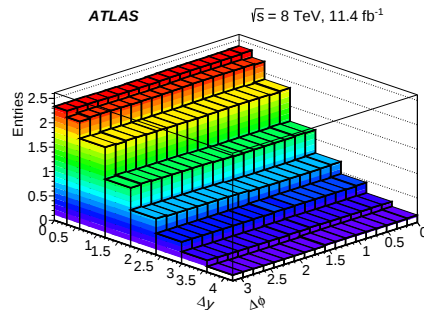


DPS

- ▶ Measure production of prompt J/ψ pairs
- ▶ Use 11.4 fb^{-1} at $\sqrt{s} = 8 \text{ TeV}$
- ▶ Kinematic range: $p_T(J/\psi) > 8.5 \text{ GeV}$, $|\eta(J/\psi)| < 2.1$
- ▶ Per-event corrections
 - ▶ Efficiency of trigger and reconstruction
 - ▶ Muon acceptance
- ▶ Backgrounds
 - ▶ Non- J/ψ background separated by 2D mass fits
 - ▶ Non-prompt J/ψ contribution separated by 2D L_{xy} fits
 - ▶ per-event weights as a function of L_{xy}
 - ▶ (Small) pile-up background separated by 1D fit to d_z vertex distance
- ▶ Due to different resolution, the measurement is done separately in central ($|\eta(J/\psi)| < 1.05$) and forward ($1.05 < |\eta(J/\psi)| < 2$) regions
- ▶ DPS and SPS contributions are distinguished with a data-driven approach

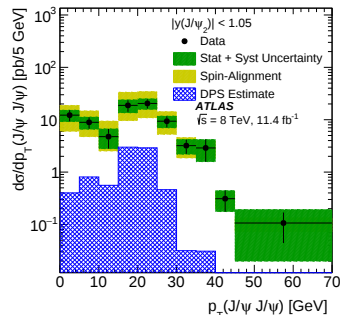
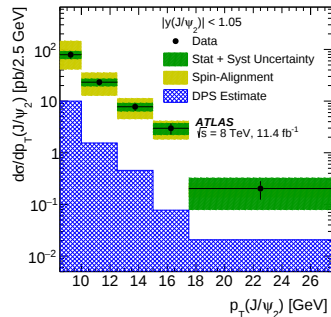
Data-driven extraction of DPS contribution

- ▶ Templates for DPS and SPS contribution in $\Delta\phi(J/\psi J/\psi) \times \Delta y(J/\psi J/\psi)$
- ▶ DPS template – event mixing
 - ▶ combine J/ψ 's from random different events, assuming their independent kinematics
 - ▶ normalize to $\Delta y > 1.8$, $\Delta\phi > \pi/2$ region
- ▶ SPS contribution
 - ▶ obtained by subtracting the DPS from data
- ▶ Per-event weights $w_{\text{DPS}}(\Delta\phi, \Delta y)$, $w_{\text{SPS}}(\Delta\phi, \Delta y)$ assigned to study the DPS/SPS spectra



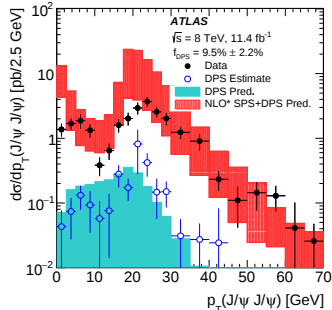
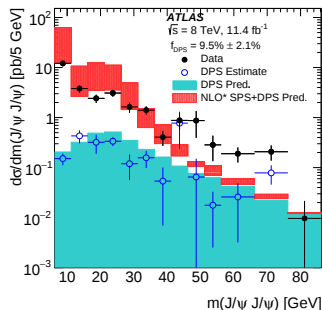
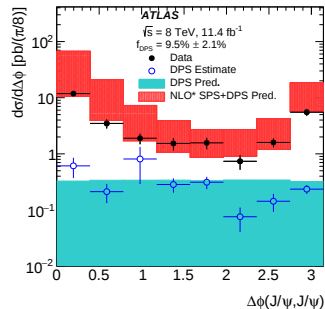
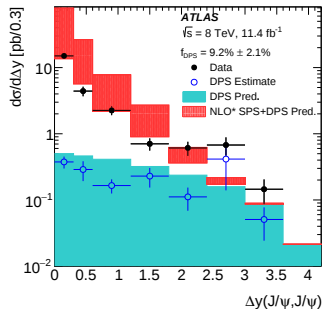
Results: cross-sections (1)

- Fiducial cross-section in $p_T(J/\psi) > 8.5$ GeV, $|y(J/\psi)| < 2.1$, $p_T(\mu) > 2.5$ GeV, $|\eta(\mu)| < 2.3$, $p_T(\mu) > 4$ GeV for two trigger muons
 15.6 ± 1.3 (stat) ± 1.2 (syst) ± 0.2 (BF) ± 0.3 (lumi) pb, for $|y| < 1.05$,
 13.5 ± 1.3 (stat) ± 1.1 (syst) ± 0.2 (BF) ± 0.3 (lumi) pb, for $1.05 \leq |y| < 2.1$
- Total cross-section in the J/ψ kinematic volume
 82.2 ± 8.3 (stat) ± 6.3 (syst) ± 0.9 (BF) ± 1.6 (lumi) pb, for $|y| < 1.05$,
 78.3 ± 9.2 (stat) ± 6.6 (syst) ± 0.9 (BF) ± 1.5 (lumi) pb, for $1.05 \leq |y| < 2.1$
 - assume unpolarized production
- Two peaks in $p_T(J/\psi J/\psi)$
 - near zero – away topology, back-to-back
 - near higher p_T – towards topology
 - back-to-back to another gluon
 - NLO effect



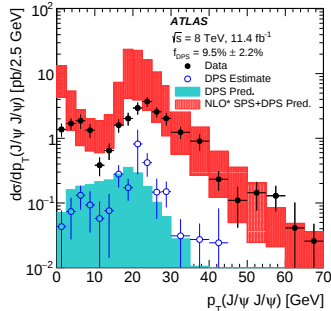
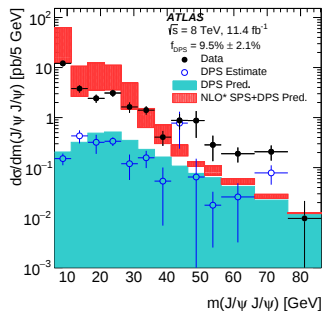
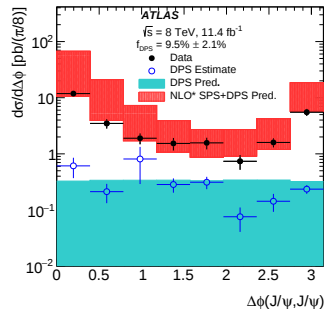
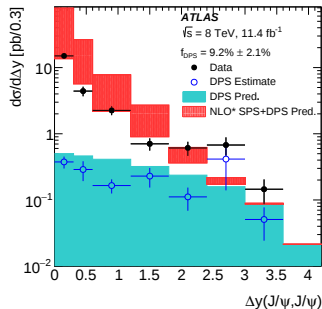
Results: cross-sections (2)

- Differential SPS/DPS cross-sections measured in the **muon fiducial volume**
- DPS: scaled to measured f_{DPS} – only shape comparison
 - LO predictions based on **Phys. Rev. D 95 (2017) 034029**
- SPS
 - Colour-Singlet NRQCD w/o loops (NLO*) **Phys. Lett. B 751 (2015) 479**, **Phys. Rev. Lett. 111 (2013) 122001**
 - Scaled by $\times 1.85$ to allow for feed-down



Results: cross-sections (2)

- Overall good agreement for DPS contribution
- Some discrepancies in total cross-section for **away** topology
- Significant fraction of events with **towards** topology $\rightarrow$ LO predictions alone not enough to describe it



Results: DPS measurements

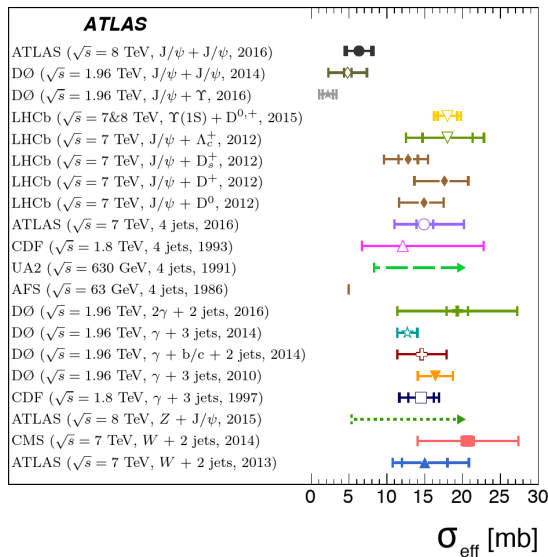
- σ_{eff} can be measured as

$$\sigma_{\text{eff}} = \frac{1}{2} \frac{\sigma(J/\psi)^2}{f_{\text{DPS}} \times \sigma(J/\psi J/\psi)}$$

- $\sigma(J/\psi)$ from the ATLAS measurement Eur. Phys. J. C 76 (2016) 283 ↗
- $f_{\text{DPS}} = (9.2 \pm 2.1(\text{stat.}) \pm 0.5(\text{syst.}))\%$
- $\sigma_{\text{DPS}} = 14.8 \pm 3.5(\text{stat.}) \pm 1.5(\text{syst.}) \pm 0.2(\text{BF}) \pm 0.3(\text{lumi.}) \text{ pb}$
- $\sigma_{\text{eff}} = 6.3 \pm 1.6(\text{stat.}) \pm 1.0(\text{syst.}) \pm 0.1(\text{BF}) \pm 0.1(\text{lumi.}) \text{ mb}$
- LHC results with quarkonia are close to each other and to those of D0, but *lower than measurements with other probes*
 - Questions the assumption of σ_{eff} universality
 - di- J/ψ , J/ψ - Υ , 4-jet processes are dominated by gg interactions
→ probe gluon distributions in proton

Experiment (energy, final state, year)

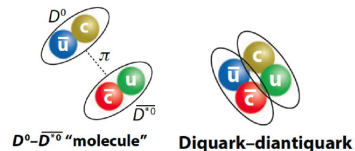
CMS ($\sqrt{s} = 8 \text{ TeV}$, $\Upsilon(1S) + \Upsilon(1S)$, 2016)
 LHCb ($\sqrt{s} = 13 \text{ TeV}$, $J/\psi + J/\psi$, 2017)
 CMS + Lansberg, Shao ($\sqrt{s} = 7 \text{ TeV}$, $J/\psi + J/\psi$, 2014)



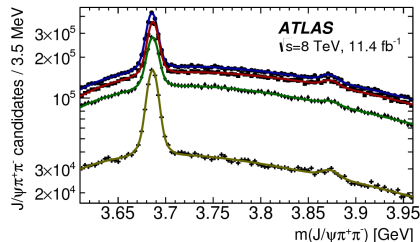
$\psi(2S)$ and $X(3872)$ production

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- ▶ $X(3872)$ was observed by Belle in 2003, later confirmed by others, $J^{PC} = 1^{++}$
- ▶ No clear theoretical picture yet
 - ▶ Loosely bound $D^0 \bar{D}^{*0}$ molecule
 - ▶ $\chi_{c1}(2P)$ state, or the mixture with $D^0 \bar{D}^{*0}$
 - ▶ Tetraquark (diquark + diquark)
- ▶ ATLAS measurement can help to answer some of the questions
 - ▶ Measure in $J/\psi \pi^+ \pi^-$ mode, together with well known $\psi(2S)$ state
 - ▶ helps to reduce systematics in ratios
 - ▶ Use 11.4 fb^{-1} @ 8 TeV data
 - ▶ Limit to $|y| < 0.75$ for the best mass resolution
 - ▶ Measure differential cross-sections over 5 p_T bins
 - ▶ Use 4 bins of pseudo proper lifetime to extract prompt/non-prompt components



- Data: $-0.3 < \tau < 0.025 \text{ ps}$ (w_0) — Fit
 - Data: $0.025 < \tau < 0.3 \text{ ps}$ (w_1) — Fit
 - Data: $0.3 < \tau < 1.5 \text{ ps}$ (w_2) — Fit
 - Data: $1.5 < \tau < 15 \text{ ps}$ (w_3) — Fit
- $12 < p_T < 16 \text{ GeV}$
 $|y| < 0.75$



X(3872) lifetime hypotheses

- Measure the $X(3872)/\psi(2S)$ ratio

$$R_B = \frac{\mathcal{B}(B \rightarrow X(3872) + \text{any}) \mathcal{B}(X(3872) \rightarrow J/\psi \pi^+ \pi^-)}{\mathcal{B}(B \rightarrow \psi(2S) + \text{any}) \mathcal{B}(\psi(2S) \rightarrow J/\psi \pi^+ \pi^-)}$$

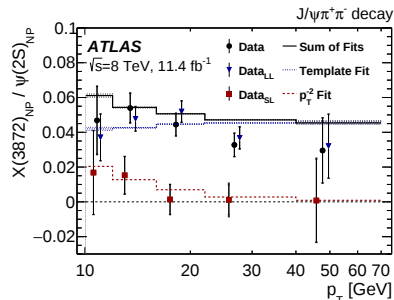
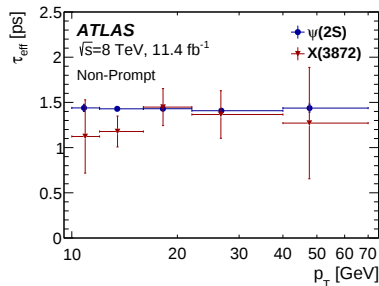
- **Single** lifetime hypothesis

- Assume non-prompt $\psi(2S)$ and $X(3872)$ produced from the same mix of parent b hadrons
- same lifetime for $\psi(2S)$ and $X(3872)$ in each p_T bin
- $R_B^{1L} = (3.95 \pm 0.32(\text{stat.}) \pm 0.08(\text{syst.})) \times 10^{-2}$
- $X(3872)$ lifetime shorter in low- p_T bins
 - Possible B_c^+ contribution?

- **Double** lifetime hypothesis: long-lived (LL) and short-lived (SL) components

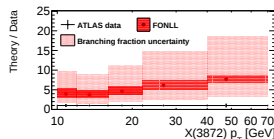
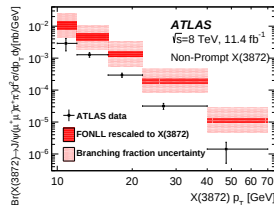
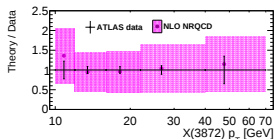
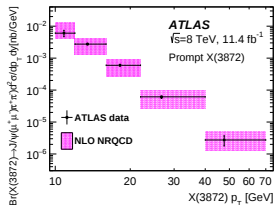
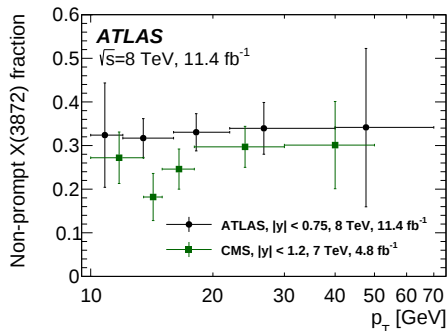
- τ_{LL} determined from $\psi(2S)$ fits, allowing for some SL contribution
- τ_{SL} from simulation, varying B_c^+ lifetime
- Calculate $X(3872)$ fraction from B_c^+

$$\frac{\sigma(pp \rightarrow B_c^+ + \text{any}) \mathcal{B}(B_c^+ \rightarrow X(3872) + \text{any})}{\sigma(pp \rightarrow \text{non-prompt } X(3872) + \text{any})} = (25 \pm 13(\text{stat.}) \pm 2(\text{syst.}) \pm 5(\text{spin}))\%$$



X(3872) production cross-section

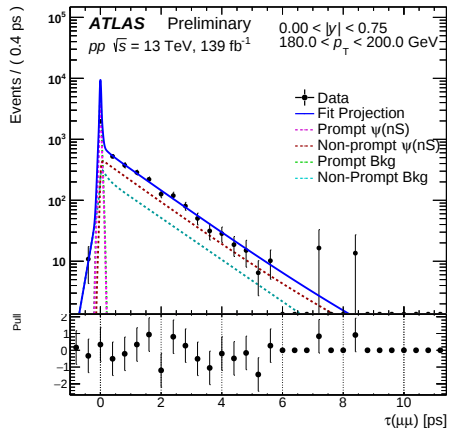
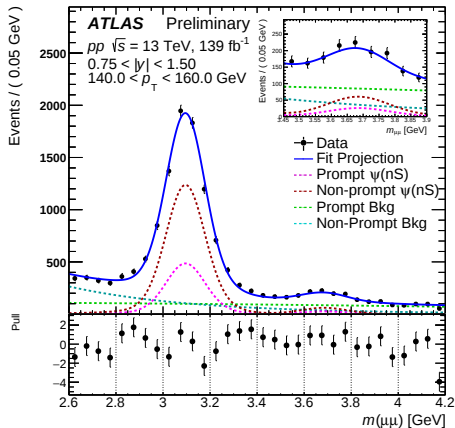
- Prompt production described well by NRQCD
 - X(3872) considered as a mixture of $\chi_c(2P)$ and $D^0\bar{D}^{*0}$ molecule
- Non-prompt compared to FONLL calculations
 - Predictions for $\psi(2S)$ recalculated using kinematic template of X(3872)/ $\psi(2S)$
 - B_s estimated from CDF data
 - Factor 4–8 above the data, larger discrepancy at high p_T
- Non-prompt production fraction: no p_T dependence, agreement with CMS data



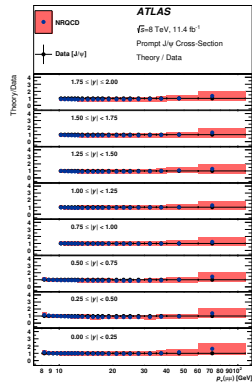
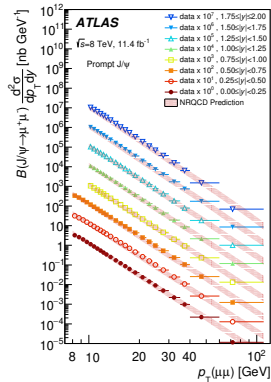
J/ψ and $\psi(2S)$ fits

i	Type	P/NP	$f_i(m)$	$h_i(\tau)$
1	J/ψ	P	$\omega G_1(m) + (1 - \omega)CB_1(m)$	$\delta(\tau)$
2	J/ψ	NP	$\omega G_1(m) + (1 - \omega)CB_1(m)$	$E_1(\tau)$
3	$\psi(2S)$	P	$\omega G_2(m) + (1 - \omega)CB_2(m)$	$\delta(\tau)$
4	$\psi(2S)$	NP	$\omega G_2(m) + (1 - \omega)CB_2(m)$	$E_2(\tau)$
5	Bkg	P	B	$\delta(\tau)$
6	Bkg	NP	$E_4(m)$	$E_5(\tau)$
7	Bkg	NP	$E_6(m)$	$E_7(\tau)$

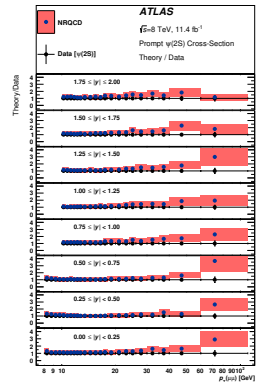
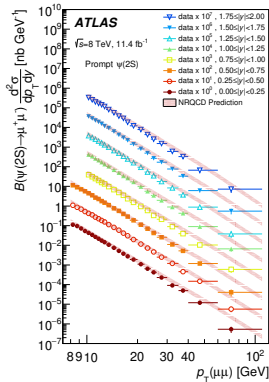
Notation	Function
G	Gaussian
CB	Crystal Ball
E	Exponential
B	Bernstein polynomials



J/ψ and $\psi(2S)$ production @ 8 TeV (Eur. Phys. J. C 76 (2016) 283): prompt



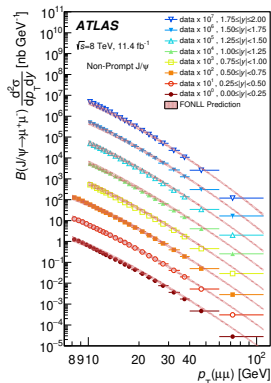
Prompt J/ψ



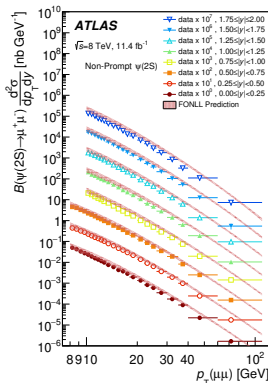
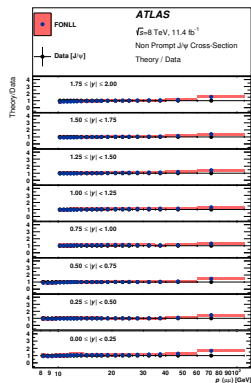
Prompt $\psi(2S)$

- ▶ J/ψ : good description by NRQCD across range of p_T , no y dependence
- ▶ $\psi(2S)$ (no significant feed-down): NRQCD mostly well describes data
 - ▶ some deterioration at high p_T

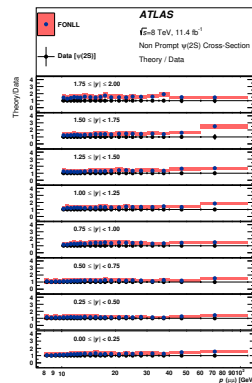
J/ψ and $\psi(2S)$ production @ 8 TeV (Eur. Phys. J. C 76 (2016) 283): non-prompt



Non-prompt J/ψ

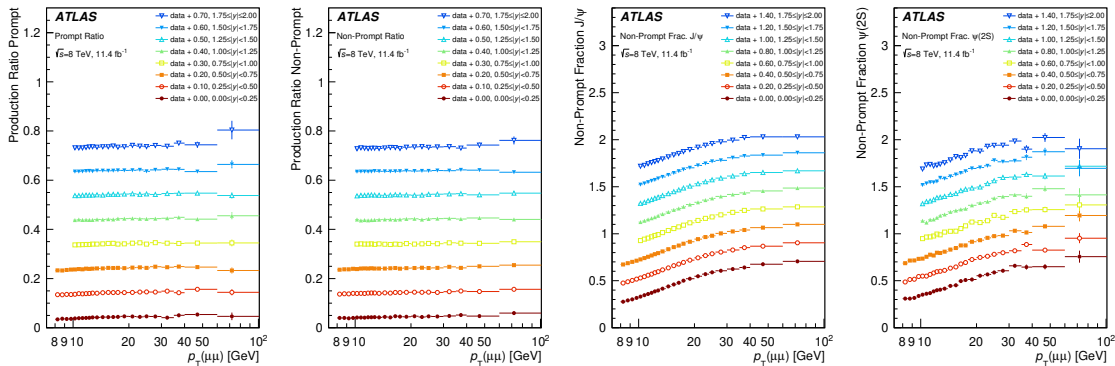


Non-prompt $\psi(2S)$



► FONLL predicts slightly harder p_T spectra for both J/ψ and $\psi(2S)$

J/ψ and $\psi(2S)$ production @ 8 TeV (Eur. Phys. J. C 76 (2016) 283): ratios



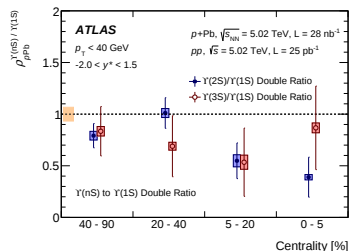
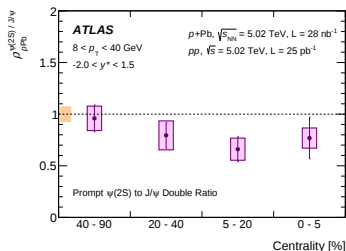
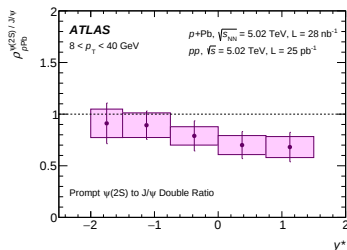
$\psi(2S)$ to J/ψ ratio for prompt/non-prompt

Non-prompt fraction for J/ψ and $\psi(2S)$

- Ratio of J/ψ to $\psi(2S)$ flat across the whole p_T range
- Prompt J/ψ ($\psi(2S)$) dominate over non-prompt at low p_T , but the non-prompt exceed after ~ 20 GeV (~ 30 GeV)

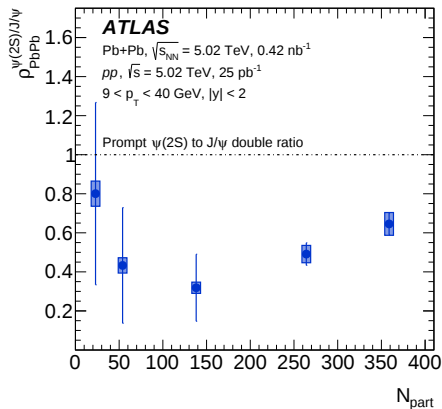
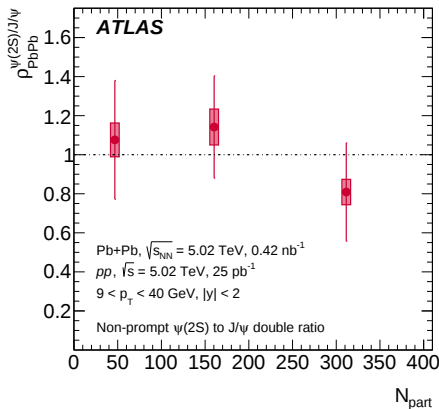
Charmonia in $p + \text{Pb}$: (nS) suppression

- Double ratios $\rho_{p\text{Pb}}^{O(nS)/O(1S)}$ in $p + \text{Pb}$
 - Relative $\psi(2S)$ suppression increases with centre-of-mass rapidity, 1σ significance trend
 - Both $\Upsilon(2,3S)$ suppressed by 2σ in the full $p_T < 40$ GeV and $-2 < y^* < 1.5$ region
 - $\rho^{\psi(2S)/\psi(1S)}$ and $\rho^{\Upsilon(2S)/\Upsilon(1S)}$ decreases towards more central collisions; $\rho^{\Upsilon(3S)/\Upsilon(1S)}$ statistically limited
 - Stronger effect of CNM in the excited states production compared to ground state

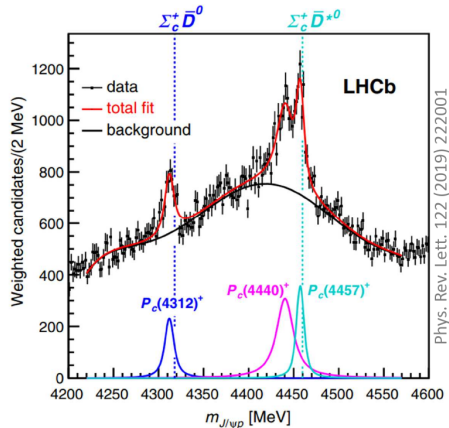
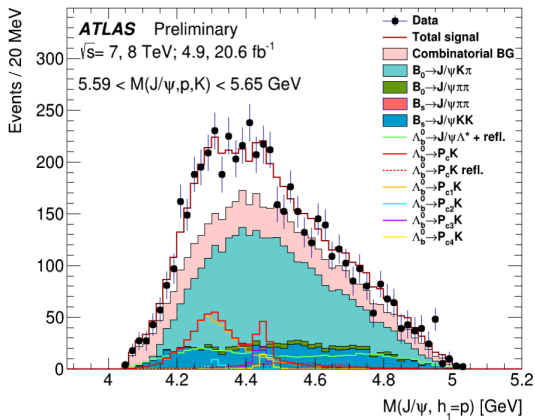


Charmonia in Pb + Pb: (nS) suppression

- ▶ Expect $\rho_{\text{PbPb}}^{O(nS)/O(1S)} = 1$ for non-prompt charmonia
 - ▶ originate from b quark losing energy in the medium and hadronizing outside
- ▶ The double ratio indeed consistent with unity for non-prompt, and < 1 for prompt
 - ▶ consistent with the interpretation that the tighter bound J/ψ survives in the hot and dense medium with higher probability than more loosely bound $\psi(2S)$
 - ▶ also consistent with radiative energy loss scenario ([Phys. Lett. B 767 \(2017\) 10](#) )



Pentaquark fit with four pentaquarks hypothesis



State	$M \text{ [MeV]}$	$\Gamma \text{ [MeV]}$	(95% CL)	$\mathcal{R} \text{ [%]}$
$P_c(4312)^+$	$4311.9 \pm 0.7_{-0.6}^{+6.8}$	$9.8 \pm 2.7_{-4.5}^{+3.7}$	(< 27)	$0.30 \pm 0.07_{-0.09}^{+0.34}$
$P_c(4440)^+$	$4440.3 \pm 1.3_{-4.7}^{+4.1}$	$20.6 \pm 4.9_{-10.1}^{+8.7}$	(< 49)	$1.11 \pm 0.33_{-0.10}^{+0.22}$
$P_c(4457)^+$	$4457.3 \pm 0.6_{-1.7}^{+4.1}$	$6.4 \pm 2.0_{-1.9}^{+5.7}$	(< 20)	$0.53 \pm 0.16_{-0.13}^{+0.15}$

Pentaquarks: event selection

- ▶ 2 muons from J/ψ decay with mass 3097 ± 290 GeV
- ▶ 2 muon tracks + 2 hadron tracks vertex fit: dimuon mass constrained to J/ψ mass, Λ_b^0 to point to primary vertex, $\chi^2/\text{n.d.f.} < 16/8$;
- ▶ 2 hadron tracks, with each of them to be assigned different mass hypothesis (proton or kaon); $p_T > 2.5$ GeV for proton candidate and $p_T > 1.8$ GeV for kaon candidate
- ▶ Transverse decay length $L_{xy}(\Lambda_b^0) > 0.7$ mm;
- ▶ $p_T(\Lambda_b^0) / \sum p_T(\text{tracks}) > 0.2$, where sum is taken over all tracks originating from PV;
- ▶ $p_T(\mu^\pm) > 4$ GeV, $|\eta(\mu^\pm)| < 2.3$, $p_T(\Lambda_b^0) > 12$ GeV, $|\eta(\Lambda_b^0)| < 2.1$;
- ▶ Inv. mass of hadron tracks (in $K\pi$ and πK mass hypotheses): $M(K\pi) > 1.55$ GeV and $M(\pi K) > 1.55$ GeV, to suppress decays via light intermediate resonances;
- ▶ $\cos\theta^*$ between proton and $J/\psi p$ system in $J/\psi p$ rest frame > -0.5 ;
- ▶ $\cos\theta^*$ between kaon and Λ_b^0 candidate in Λ_b^0 candidate rest frame > -0.8 ;
- ▶ $|\cos\theta^*|$ between kaon and Λ^{*0} in Λ^{*0} rest system < 0.85 ;
- ▶ Events for $J/\psi p$ signal search are taken in window $M(J/\psi pK) \in 5620 \pm 30$ MeV;
- ▶ Subtraction of distributions with two same sign hadron tracks is applied before fits to data;

Systematics in the D meson measurement

Source	$\sigma^{\text{vis}}(D^{*\pm})$		$\sigma^{\text{vis}}(D^{\pm})$		$\sigma^{\text{vis}}(D_s^{\pm})$	
	Low- p_T	High- p_T	Low- p_T	High- p_T	Low- p_T	High- p_T
Trigger (δ_1)	-	$+0.9\%$ -1.0%	-	$+0.9\%$ -1.0%	-	$+0.9\%$ -1.0%
Tracking (δ_2)	$\pm 7.8\%$	$\pm 7.4\%$	$\pm 7.7\%$	$\pm 7.4\%$	$\pm 7.6\%$	$\pm 7.4\%$
D selection (δ_3)	$+2.8\%$ -1.6%	$+1.7\%$ -1.4%	$+1.6\%$ -1.0%	$+0.9\%$ -0.6%	$+2.6\%$ -1.6%	$+1.1\%$ -0.9%
Signal fit (δ_4)	$\pm 1.3\%$	$\pm 0.9\%$	$\pm 1.3\%$	$\pm 1.5\%$	$\pm 6.4\%$	$\pm 5.3\%$
Modelling (δ_5)	$+1.0\%$ -1.7%	$+2.7\%$ -2.3%	$+2.3\%$ -2.6%	$+2.9\%$ -2.4%	$+1.7\%$ -2.4%	$+2.8\%$ -2.4%
Size of MC sample (δ_6)	$\pm 0.6\%$	$\pm 0.9\%$	$\pm 0.8\%$	$\pm 0.8\%$	$\pm 2.9\%$	$\pm 3.1\%$
Luminosity (δ_7)	$\pm 3.5\%$	$\pm 3.5\%$	$\pm 3.5\%$	$\pm 3.5\%$	$\pm 3.5\%$	$\pm 3.5\%$
Branching fraction (δ_8)	$\pm 1.5\%$	$\pm 1.5\%$	$\pm 2.1\%$	$\pm 2.1\%$	$\pm 5.9\%$	$\pm 5.9\%$

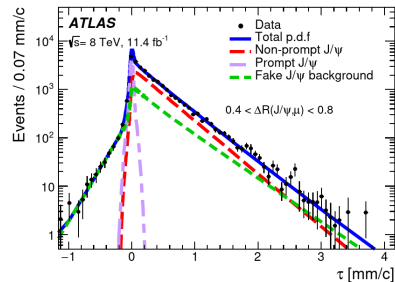
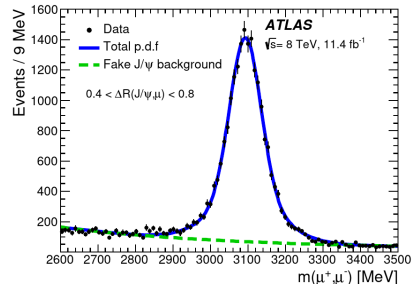
	LEP data
$f(c \rightarrow D^{*+})$	$0.236 \pm 0.006 \pm 0.003$
$f(c \rightarrow D^+)$	$0.225 \pm 0.010 \pm 0.005$
$f(c \rightarrow D_s^+)$	$0.092 \pm 0.008 \pm 0.005$
$f(b \rightarrow D^{*\pm})$	$0.221 \pm 0.009 \pm 0.003$
$f(b \rightarrow D^\pm)$	$0.223 \pm 0.011 \pm 0.005$
$f(b \rightarrow D_s^\pm)$	$0.138 \pm 0.009 \pm 0.006$

Option label	Descriptions
Opt. 1	The same splitting kernel, $(1/2)(z^2 + (1 - z)^2)$, for massive as massless quarks, only with an extra β phase-space factor. This was the default setting in PYTHIA8.1, and currently must also be used with the MC@NLO [50] method.
Opt. 4	A splitting kernel $z^2 + (1 - z)^2 + 8r_q z(1 - z)$, normalised so that the z -integrated rate is $(\beta/3)(1 + r/2)$, and with an additional suppression factor $(1 - m_{qq}^2/m_{\text{dipole}}^2)^3$, which reduces the rate of high-mass $q\bar{q}$ pairs. This is the default setting in PYTHIA8.2.
Opt. 5	Same as Option 1, but reweighted to an $\alpha_s(km_{qq}^2)$ rather than the normal $\alpha_s(p_T^2)$, with $k = 1$.
Opt. 5b	Same as Option 5, but setting $k = 0.25$.
Opt. 8	Same as Option 4, but reweighted to an $\alpha_s(km_{qq}^2)$ rather than the normal $\alpha_s(p_T^2)$, with $k = 1$.
Opt. 8b	Same as Option 8, but setting $k = 0.25$.

Table 1: Description of PYTHIA8 options. Options 2, 3, 6 and 7 are less well physically motivated and not considered here. The notation used is as follows: $r_q = m_q^2/m_{qq}^2$, $\beta = \sqrt{1 - 4r_q}$, with m_q the quark mass and m_{qq} the $q\bar{q}$ pair invariant mass.

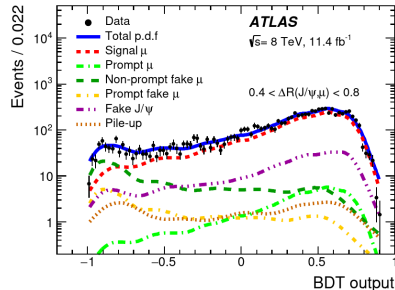
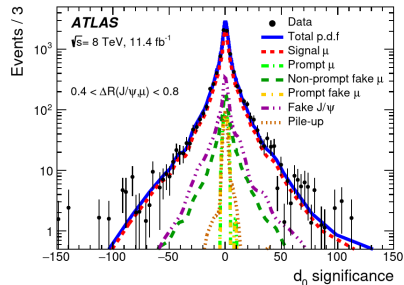
$b\bar{b}$ production measurement details

- Fiducial volume definition:
 - $p_T(\mu) > 6$ GeV for all three muons
 - $|\eta(\mu)| < 2.3$ for the J/ψ muons and < 2.5 for the 3rd muon
- Signal extraction, in each bin
 - Simultaneous fit to J/ψ mass and pseudo-proper lifetime to extract the yield of J/ψ from b



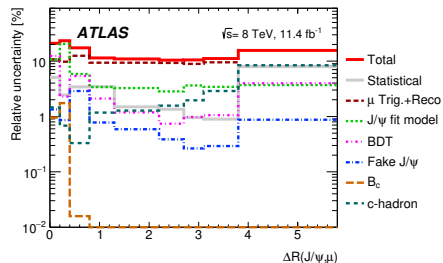
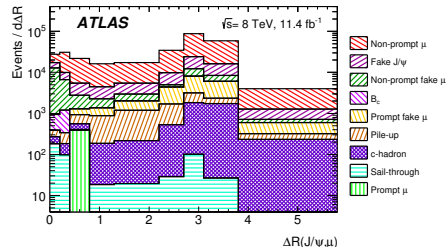
$b\bar{b}$ production measurement details

- ▶ Fiducial volume definition:
 - ▶ $p_T(\mu) > 6 \text{ GeV}$ for all three muons
 - ▶ $|\eta(\mu)| < 2.3$ for the J/ψ muons and < 2.5 for the 3rd muon
- ▶ Signal extraction, in each bin
 - ▶ Simultaneous fit to J/ψ mass and pseudo-proper lifetime to extract the yield of J/ψ from b
 - ▶ Yield of 3rd muon from b determined by fit to $d_0/\sigma(d_0)$ and BDT output
 - ▶ in signal-enriched region of $\tau > 0.25 \text{ mm}/c$



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 - ▶ in signal-enriched region of $\tau > 0.25 \text{ mm}/c$
 - ▶ Subtract irreducible backgrounds
 - ▶ $B_c^+ \rightarrow J/\psi \mu^+ X$, prompt charm, fake muons



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 - ▶ in signal-enriched region of $\tau > 0.25 \text{ mm}/c$
 - ▶ Subtract irreducible backgrounds
 - ▶ $B_c^+ \rightarrow J/\psi \mu^+ X$, prompt charm, fake muons
 - ▶ Extrapolate to full τ range
 - ▶ Correct for detector resolution effects

